

# 1. Givens rotations

A Givens rotation is represented by a matrix of the form

$$G(i,j,\theta) = \begin{bmatrix} 1 & \dots & 0 & \dots & 0 & \dots & 0 \\ \vdots & \ddots & \vdots & & \vdots & & \vdots \\ 0 & \dots & c & \dots & -s & \dots & 0 \\ \vdots & & \vdots & \ddots & \vdots & & \vdots \\ 0 & \dots & s & \dots & c & \dots & 0 \\ \vdots & & \vdots & & \vdots & \ddots & \vdots \\ \vdots & & \vdots & & \vdots & & \vdots \\ 0 & \dots & 0 & \dots & 0 & \dots & 1 \end{bmatrix}, \quad (1.1)$$

which is, when  $i > j$ ,

$$G_{kk} = 1 \text{ for } k \neq i,j, \quad G_{ii} = G_{jj} = \cos(\theta), \quad G_{ji} = -G_{ij} = -\sin(\theta). \quad (1.2)$$

(See [https://en.wikipedia.org/wiki/Givens\\_rotation](https://en.wikipedia.org/wiki/Givens_rotation).)